

DEPARTMENT OF PHYSICS				CLASS: I M.Sc. Physics				
Sem	Course Type	Course Code	Course Title	Credits	Contact Hours/week	CIA	Ext	Total
II	Major Core-4	21P2PMC4	Mathematical Physics - II	4	5	25	75	100

Nature of Course			
Knowledge and skill	✓		Employability oriented
Skill oriented			Entrepreneurship oriented

Course Objectives :

- To highlight the relationship of mathematical tools to understanding the dynamics of the physical world we live in.
- To impart knowledge on mathematical tools and techniques that could model real life physical systems.
- To demonstrate the use of Complex analysis and integration, tensor analysis and group theory in areas like Electromagnetic theory, Quantum Mechanical systems and crystallographic systems.

Course Content:

Unit	Description	Hours	K-level	CLO
I	Complex variables-I : Analytic function – Cauchy Reiman equations – CR in polar form – Complex line integral – Cauchy integral theorem (simple proof) – cauchy integral formula – Derivative of an analytic function (n^{th} derivative) – Expansion of an analytic function.	15	Up to K3	1
II	Complex variables-II : Singular point – Isolated singularity – Removal singularity – Cauchy-Residue theorem – Residue – Calculation of residue at simple poles and poles of higher order – Evaluation of definitive integrals – Integration around unit circle – Jordan lemma – Semicircular contours – Poles on the real axis.	15	Up to K4	2
III	Tensors : Scalar, vector and tensors – difference between a tensor and a transformation matrix – second rank tensor – Definition – Examples – Contra variant, covariant and mixed tensors – Tensors – Equality and null tensors- addition, subtraction, outer product and inner product-metric tensor-Tensors in EM theory	15	Up to K2	3
IV	Crystal symmetry and Abstract Group theory : Crystal symmetry operators – The crystallographic point groups – stereographic projection of simple point groups – classification of point groups according to crystal systems – Definition of groups – Group multiplication table – Multiplication tables for C_{2v} , C_{3v} , C_3 , C_4 , C_2 point groups – Rearrangement theorem – Cyclic groups –	15	Up to K4	4

	Subgroups – Cosets – Example groups of finite order – Conjugate elements and class structure – physical interpretation of class structure – Normal divisors and factor groups – isomorphy and homomorphy – class multiplication.			
V	Theory of Group Representations and construction of character tables : Definitions – reducible and irreducible representations – Lemma I, II and III with proof – Great orthogonal theorem – Character of a representation – Construction of character tables – Decomposition of regular representations.	15	Up to K3	5

Books for study :

1. Mathematical Physics with Classical Mechanics, Satyaprakash, Sultan Chand & sons, New Delhi, Vth edition, 2009 – Unit I: 6.9, 6.10, 6.12, 6.14, 6.16, 6.17.
2. Mathematical Physics with Classical Mechanics, Satyaprakash, Sultan Chand & sons, New Delhi, Vth edition, 2009 – Unit II: 6.22, 6.23, 6.24, 6.25(a), 6.25(b), 6.25(c), 6.25(d).
3. Vector analysis and Tensor analysis – M.R. Spiegel, Schaum's outline series, MH, 1974
Unit III – chapter 8.
4. Group theory and quantum mechanics, Michael Tinkam, 2003.
Unit IV – Chapter 2.1-2.9, 4.1, 4.2; Unit V – Chapter 3.1-3.5.

Books for reference :

1. Chemical Applications of Group theory, Albert F Cotton, Wiley Inc., III Edition, 2008
2. Mathematical Methods for Physicists, Arfken & Weber, VI Edition, Elsevier, 2011
3. Mathematical methods in Physical Sciences, Mary L Boas, Wiley Eastern, III Edition, 2006
4. Mathematical methods for Physicists and Engineers, Riley, Hobson and Bence, Cambridge University Press, III Edition, 2018.

Web Resources :

1. [https://chem.libretexts.org/Bookshelves/Physical_and_Theoretical_Chemistry_Textbook_Maps/Supplemental_Modules_\(Physical_and_Theoretical_Chemistry\)/Group_Theory/Group_Theory_and_its_Application_to_Chemistry](https://chem.libretexts.org/Bookshelves/Physical_and_Theoretical_Chemistry_Textbook_Maps/Supplemental_Modules_(Physical_and_Theoretical_Chemistry)/Group_Theory/Group_Theory_and_its_Application_to_Chemistry)
2. <https://ocw.mit.edu/resources/res-3-004-visualizing-materials-science-fall-2017/student-projects-by-year/EPFL2017/crystallographic-point-groups/a-visualisation-of-crystallographic-point-groups/>
3. <https://www.sjsu.edu/faculty/watkins/tensor1.htm>
4. <https://nptel.ac.in/courses/111/103/111103070/>

Pedagogy :

Chalk and talk, Presentation, Quiz, Seminar, Assignment

Course Designers :

S. Sivaramakrishnan

Dr. K. Neyvasagam

Course Plan :

Unit	Topics	Hrs	Mode
Unit I	Analytic function	3	Chalk and talk, Presentation, Quiz and assignment
	Cauchy Reiman equations – CR in polar form –	3	
	Complex line integral – Cauchy integral theorem (simple proof)	3	
	cauchy integral formula – Derivative of an analytic function (n^{th} derivative) – Expansion of an analytic function	3	
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Unit II	Singular point – Isolated singularity – Removal singularity	3	Chalk and talk, Quiz and assignment
	Cauchy-Residue theorem – Residue – Calculation of residue at simple poles and poles of higher order	3	
	Evaluation of definitive integrals – Integration around unit circle	3	
	Jordan lemma	3	
	Semicircular contours – Poles on the real axis	3	
Unit III	Scalar, vector and tensors	3	Chalk and talk, Quiz, assignment and seminar
	Difference between a tensor and a transformation matrix – second rank tensor – Definition – Examples	5	
	Contra variant, covariant and mixed tensors – Tensors – Equality and null tensors- addition, subtraction, outer product and inner product-metric tensor	4	
	Tensors in EM theory	3	
Unit IV	Crystal symmetry operators	3	Chalk and talk, quiz, Seminar
	The crystallographic point groups – stereographic projection of simple point groups – classification of point groups according to crystal systems	3	
	Definition of groups – Group multiplication table – Multiplication tables for C_{2v} , C_{3v} , C_3 , C_4 , C_2 point groups	3	
	Rearrangement theorem – Cyclic groups – Subgroups	1	
	Cosets – Example groups of finite order	1	
	Conjugate elements and class structure – physical interpretation of class structure – Normal divisors and factor groups	2	
	Isomorphy and homomorphy – class multiplication.	2	
Unit V	Definitions – reducible and irreducible representations	2	Chalk and talk, Quiz, Presentation, Seminar
	Lemma I, II and III with proof – Great orthogonal theorem	5	
	Character of a representation	2	
	Construction of character tables – Decomposition of regular representations.	6	

Course learning Outcomes:

On the successful completion of the course, students will be able to

CLOs	Course Learning Outcomes	Knowledge Level
CLO-1	Apply Cauchy-Riemann equation and Cauchy's integral theorem to analytic function.	Up to K3
CLO-2	Analyze poles and residues using concepts of contour integration.	Up to K4
CLO-3	Understanding the application of tensors in Physics.	Up to K2
CLO-4	Classify molecules among various crystallographic point groups by applying principles of group theory.	Up to K4
CLO-5	Apply the Great Orthogonality theorem to crystallographic point groups and construct character tables.	Up to K3

Mapping of CLOs with PSOs :

#	PSO1	PSO2	PSO3	PSO4	PSO5
CLO1	3	3		2	1
CLO2	3	3		2	1
CLO3	3	3		2	1
CLO4	3	3		2	1
CLO5	3	3		2	1

Advance application –3, Intermediate level –2 , Basic level–1

Learning Outcome Based Education (LOBE) & Assessment
Summative Examination – Blue Print
Articulation Mapping-K Levels with Courses Learning Outcomes (CLOs)

Units	CLOs	K- Level	Section A		Section B		Section C (Either/or Choice)	Section D (Open Choice)
			MCQs		Short Answers			
			No. of Questions	K- Level	No. of Questions	K- Level		
1	CLO 1	Up to K3	2	K3& K3	1	K3	2 (K3&K3)	1 (K2)
2	CLO 2	Up to K4	2	K2 & K3	1	K4	2 (K1&K1)	1 (K3)
3	CLO 3	Up to K2	2	K1 & K1	1	K1	2 (K4&K4)	1 (K4)
4	CLO 4	Up to K4	2	K4 & K4	1	K4	2 (K4&K4)	1 (K4)
5	CLO 5	Up to K3	2	K2 & K3	1	K2	2 (K2&K2)	1 (K3)
No. of Questions to be asked			10			5	10	5
No. of Questions to be answered			10			5	5	3
Marks for each question			1			2	5	10
Total Marks for each section			10			10	25	30

Distribution of Section-wise Marks with K Levels

K Levels	Section A (No Choice)	Section B (No Choice)	Section C (Either/or)	Section D (Open Choice)	Total Marks	% of Marks without choice
K1	2	4	10	-	16	13.33
K2	2	4	10	10	26	21.67
K3	4	2	10	20	36	30.00
K4	2	-	20	20	42	35.00
Total Marks	10	10	50	50	120	100.00